Co-movements of and Linkages between Asian Stock Markets

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\textbf{Abstract:} International marketers may be interested in stock market linkages for various reasons: the co-movements of equity prices appear to reflect not only market globalization but also the globalization of capital resources. The co-movements can affect the balancing strategies of country market portfolios as they indicate opportunities and risks. The strategic choice of alternative market presence, such as market entry via export marketing or a full ownership and marketing may need to match with the type of financial resources. The co-movements of and the linkages between the U.S. stock market and Asian stock markets have been studied extensively. However, little attention has been given to the co-movements of Asian stock markets and the lead/lag linkages between them. In this paper, we study this issue with the principal components analysis (PCA) and Granger causality (G-C) statistical techniques. We find that the contemporaneous co-movements of Asian stock markets have become closer and portfolio diversification benefits with Asian stock markets have diminished over time during the January 1, 2001-January 1, 2011 period. We find that the Singapore, Indian, and Japanese stock markets are the most influential stock markets and the Philippine and South Korean stock markets are the least influential stock markets in Asia. The Japanese, Singapore, and New Zealand stock markets are the least affected stock markets and the Shanghai, Australian, and South Korean stock markets are the most affected stock markets by the movements in the other Asian stock markets.

\textbf{Keywords:} Asian stock markets, Co-movements of stock markets, Linkages between stock markets, Principal components analysis, Granger causality

\textbf{JEL Classification:} G11, G15

1. Introduction

In this paper, we study the contemporaneous co-movements of Asian stock markets and the time series lead/lag linkages between them with the principal components analysis (PCA) and Granger causality (G-C) statistical techniques with a sample of thirteen major Asian stock markets during the January 1, 2001-January 1, 2011 period.

Studying the contemporaneous co-movements of national stock markets has long been a popular research topic in finance (see: Meric and Meric, 2011). Makridakis and Wheelwright (1974), Philippatos, Christofi, and Christofi (1983), and Meric and Meric (1989) have made the use of the PCA multivariate technique popular in studying the co-movements of national stock markets. The technique has since been used in many studies (see, eg., Lee and Kim, 1993; Lau and McLnish, 1993; Meric and Meric, 1996, 1997, 2001a,b). In this paper, we use the PCA techniques to study the contemporaneous co-movement patterns of Asian stock markets with daily index returns data for the January 1, 2001-January 1, 2011 period.
We divide the 10-year period into two 5-year sub-periods and we apply PCA to each period to determine if there are significant changes in the co-movement patterns of Asian stock markets over time.

In empirical studies, the G-C technique is often used to determine if the past index returns of a national stock market can be used to predict the future index returns of other national stock markets (see, e.g., Ratner and Leal, 1996; Meric et al., 2002; Meric and Meric, 2011). In this paper, we use the G-C technique to study the lead/lag linkages between Asian stock markets with daily stock market index data for the January 1, 2001-January 1, 2011 period. We determine the most influential and the least influential stock markets in Asia. We investigate which Asian stock markets are leading the others and which Asian stock markets tend to follow the others. We determine the Asian stock markets that are most affected and those that are least affected by the movements of the other Asian stock markets.

The paper is organized as follows. In the next section, we explain our data and methodology. We present our PCA results in Section III. We present our G-C analysis results in Section IV. We summarize our findings and present our conclusions in Section V. We describe the PCA and G-C statistical techniques in Appendixes A and B, respectively.

2. Data and Methodology

The study covers the following thirteen Asian stock markets: Australia, Hong Kong, India, Indonesia, Japan, Malaysia, New Zealand, the Philippines, Singapore, Shanghai, South Korea, Taiwan, and Thailand. The daily stock market indexes for these stock markets were downloaded from the DataStream database. The Morgan Stanley Capital International (MSCI) data are used for the Indonesian and South Korean stock markets. The DataStream data are used for the other stock markets. The daily stock returns were computed as the log difference in the indexes \( \ln \left( \frac{I_t}{I_{t-1}} \right) \).

The principal component analysis (PCA) is a widely used multivariate statistical technique to study the contemporaneous co-movements of global equity markets. The PCA technique can combine global stock markets into distinct principal component clusters in terms of the similarities of their contemporaneous co-movements. Stock markets with correlated, close co-movement patterns are not good portfolio diversification prospects. We determine which Asian stock markets were good portfolio diversification prospects for investors during the January 1, 2001-January 1, 2011 period. We use the PCA technique to study the contemporaneous co-movement patterns of the Asian stock markets. A brief description of the PCA techniques is presented in Appendix A. A detailed discussion of the technique can be found in Mardia, Kent, and Bibby (1979) and Marascuilo and Levin (1983).

An independent variable \( X \) Granger-causes a change in dependent variable \( Y \), if \( Y \) can be better forecasted with past values of both \( X \) and \( Y \) than just with past values of \( Y \) alone (see: Granger, 1969, 1988). The causality in the Granger sense does not imply a cause and effect relationship, but one of predictability. In empirical studies, the Granger-causality (G-C) technique is often used to determine if the index returns of a national stock market can predict the future index returns of other national stock markets (see, e.g., Ratner and Leal, 1996; Meric et al., 2002). A brief description of the G-C technique is presented in Appendix B. In this paper, we use the G-C technique to study if the past daily index returns of the thirteen Asian stock markets covered in the study could be used to predict each other's future daily index returns during the January 1, 2001-January 1, 2011 period. We investigate which Asian
stock markets are leading the other Asian stock markets and which Asian stock markets are affected the most by the movements in the other Asian stock markets. Stock markets with significant lead/lag linkages are not good portfolio diversification prospects for investors.

3. Principal Components Analysis

To determine the clusters of stock markets with similar contemporaneous movement patterns, the correlation matrix of the thirteen Asian stock markets was used as input in the SPSS-PCA program. The Varimax rotation was used to maximize the factor loadings of the stock markets in each principal component with similar movement patterns. Using Kaiser's significance rule, statistically significant principal components with eigenvalues greater than unity were retained for analysis (see: Mardia et al., 1979, Marascuilo and Levin, 1983). The January 1, 2001-January 1, 2011 ten-year period was divided into two five-year sub-periods and the analysis was applied to each sub-period separately.

3.1. January 1, 2001-January 1, 2006 Period

There are three statistically significant principal components for this period. The highest factor loadings for the thirteen stock markets in the three principal components are presented in Table 1. The stock markets with high factor loadings in the same principal component have similar contemporaneous movement patterns and they are highly correlated. Therefore, having these stock markets in the same investment portfolio would provide limited diversification benefits. To maximize the portfolio diversification benefit, investors should invest in the stock markets with high factor loadings in different principal components.

<table>
<thead>
<tr>
<th>Stock Markets</th>
<th>Factor Loadings</th>
<th>Principal Comp. #1</th>
<th>Principal Comp. #2</th>
<th>Principal Comp. #3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hong Kong</td>
<td>0.783</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>South Korea</td>
<td>0.689</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Singapore</td>
<td>0.666</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Shanghai</td>
<td>0.647</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Taiwan</td>
<td>0.638</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>India</td>
<td>0.535</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Japan</td>
<td>0.532</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Thailand</td>
<td>0.404</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>New Zealand</td>
<td></td>
<td>0.891</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Australia</td>
<td></td>
<td></td>
<td>0.849</td>
<td></td>
</tr>
<tr>
<td>The Philippines</td>
<td></td>
<td></td>
<td></td>
<td>0.739</td>
</tr>
<tr>
<td>Malaysia</td>
<td></td>
<td></td>
<td></td>
<td>0.625</td>
</tr>
<tr>
<td>Indonesia</td>
<td></td>
<td></td>
<td></td>
<td>0.572</td>
</tr>
<tr>
<td>Eigenvalue</td>
<td>4.563</td>
<td>1.272</td>
<td>1.049</td>
<td></td>
</tr>
<tr>
<td>Variance Explained</td>
<td>35.1%</td>
<td>9.8%</td>
<td>8.1%</td>
<td></td>
</tr>
<tr>
<td>Cum. Variance Exp.</td>
<td>35.1%</td>
<td>44.9%</td>
<td>53.0</td>
<td></td>
</tr>
</tbody>
</table>

The first principal component is dominated by the Hong Kong, South Korean, Singapore, Shanghai, Taiwanese, Indian, Japanese, and Thai stock markets. This principal component has an eigenvalue of 4.563 and it explains 35.1 percent of the variation in the original data matrix. The New Zealand and Australian stock markets have their highest factor loadings in the second principal component. This principal component has an eigenvalue of 1.272 and it
explains 9.8 percent of the variation in the original data matrix. The Philippine, Malaysian, and Indonesian stock markets have their highest factor loadings in the third principal component. This principal component has an eigenvalue of 1.049 and it explains 8.1 percent of the variation in the original data matrix. All three principal components together can explain 53.0 percent of the variance in the original data matrix.

3.2. January 1, 2006-January 1, 2011 period

The analysis is also applied to the January 1, 2006-January 1, 2011 period to determine if there are any significant changes in the contemporaneous co-movement patterns of Asian stock markets over time. This time period includes the 2008 global stock market crash and the post-crash recovery in 2009, when all global stock markets moved closely together. Therefore, one would expect that the number of statistically significant principal components would decrease and the benefits of global portfolio diversification would diminish during this period.

Indeed, there is only one statistically significant principal component for the January 1, 2006-January 1, 2011 period. The factor loadings of the principal component are presented in Table 2. The principal component has an eigenvalue of 7.638 and it explains 58.8 percent of the variation in the original data matrix.

<table>
<thead>
<tr>
<th>Stock Markets</th>
<th>Factor Loadings of the Principal Component</th>
</tr>
</thead>
<tbody>
<tr>
<td>Singapore</td>
<td>0.891</td>
</tr>
<tr>
<td>Hong Kong</td>
<td>0.882</td>
</tr>
<tr>
<td>Australia</td>
<td>0.847</td>
</tr>
<tr>
<td>Shanghai</td>
<td>0.826</td>
</tr>
<tr>
<td>South Korea</td>
<td>0.806</td>
</tr>
<tr>
<td>Malaysia</td>
<td>0.768</td>
</tr>
<tr>
<td>Taiwan</td>
<td>0.765</td>
</tr>
<tr>
<td>Indonesia</td>
<td>0.753</td>
</tr>
<tr>
<td>The Philippines</td>
<td>0.699</td>
</tr>
<tr>
<td>New Zealand</td>
<td>0.693</td>
</tr>
<tr>
<td>India</td>
<td>0.678</td>
</tr>
<tr>
<td>Thailand</td>
<td>0.655</td>
</tr>
<tr>
<td>Japan</td>
<td>0.646</td>
</tr>
<tr>
<td>Eigenvalue</td>
<td>7.638</td>
</tr>
<tr>
<td>Var. Explained</td>
<td>58.8%</td>
</tr>
</tbody>
</table>

There are three statistically significant principal components in the January 1, 2001-January 1, 2006 period versus only one statistically significant principal component in the January 1, 2006-January 1, 2011 period. This indicates that the co-movements of Asian stock markets became considerably closer and the portfolio diversification benefits of investing in Asian stock markets decreased significantly from the first five-year period to the second five-year period.
4. Granger-Causality Tests

The Estima RATS Granger-Sims computer program was used in the Granger causality (G-C) tests. The optimal lag-length is three trading days in the VAR system used in the analysis (see: Sims, 1980). The G-C test results for the joint hypotheses of zero coefficients on all three lags for each stock market are presented in Table 3.

Table 3. Granger-Causality Test Statistics: January 1, 2001-January 1, 2011

<table>
<thead>
<tr>
<th>Dependent Variable</th>
<th>AU</th>
<th>HO</th>
<th>IN</th>
<th>ID</th>
<th>JA</th>
<th>MA</th>
<th>NZ</th>
<th>PH</th>
<th>SH</th>
<th>SI</th>
<th>SK</th>
<th>TA</th>
<th>TH</th>
</tr>
</thead>
<tbody>
<tr>
<td>AU</td>
<td>0.3</td>
<td>11*</td>
<td>0.7</td>
<td>10*</td>
<td>10*</td>
<td>6*</td>
<td>1.8</td>
<td>1.2</td>
<td>20*</td>
<td>1.6</td>
<td>3**</td>
<td>3**</td>
<td></td>
</tr>
<tr>
<td>HO</td>
<td>1.8</td>
<td>9*</td>
<td>1.7</td>
<td>18*</td>
<td>7*</td>
<td>14*</td>
<td>1.1</td>
<td>6*</td>
<td>24*</td>
<td>0.7</td>
<td>4*</td>
<td>0.6</td>
<td></td>
</tr>
<tr>
<td>IN</td>
<td>4*</td>
<td>1.7</td>
<td>2.3</td>
<td>5*</td>
<td>2.3</td>
<td>8*</td>
<td>0.4</td>
<td>6*</td>
<td>3**</td>
<td>7*</td>
<td>1.5</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>ID</td>
<td>1.4</td>
<td>1.8</td>
<td>12*</td>
<td>5*</td>
<td>8*</td>
<td>6*</td>
<td>0.9</td>
<td>4*</td>
<td>11*</td>
<td>1.4</td>
<td>11</td>
<td>3**</td>
<td></td>
</tr>
<tr>
<td>JA</td>
<td>0.9</td>
<td>0.7</td>
<td>6*</td>
<td>0.2</td>
<td>3**</td>
<td>3**</td>
<td>1.5</td>
<td>0.4</td>
<td>13*</td>
<td>0.1</td>
<td>0.3</td>
<td>3**</td>
<td></td>
</tr>
<tr>
<td>MA</td>
<td>1.4</td>
<td>2.2</td>
<td>19*</td>
<td>2.2</td>
<td>8*</td>
<td>3**</td>
<td>2.5</td>
<td>6*</td>
<td>10*</td>
<td>0.7</td>
<td>3**</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
<td>NZ</td>
<td>5*</td>
<td>0.7</td>
<td>3**</td>
<td>0.8</td>
<td>6*</td>
<td>3**</td>
<td>1.0</td>
<td>0.7</td>
<td>10*</td>
<td>1.2</td>
<td>1.2</td>
<td>4*</td>
<td></td>
</tr>
<tr>
<td>PH</td>
<td>4*</td>
<td>1.1</td>
<td>10*</td>
<td>3**</td>
<td>8*</td>
<td>1.3</td>
<td>8*</td>
<td>0.1</td>
<td>14*</td>
<td>0.8</td>
<td>3**</td>
<td>4*</td>
<td></td>
</tr>
<tr>
<td>SH</td>
<td>1.1</td>
<td>7*</td>
<td>10*</td>
<td>1.7</td>
<td>15*</td>
<td>5*</td>
<td>11*</td>
<td>1.2</td>
<td>16*</td>
<td>2.0</td>
<td>3**</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
<td>SI</td>
<td>2.3</td>
<td>0.2</td>
<td>6*</td>
<td>0.1</td>
<td>8*</td>
<td>5*</td>
<td>6*</td>
<td>1.4</td>
<td>3**</td>
<td>0.4</td>
<td>2.3</td>
<td>0.4</td>
<td></td>
</tr>
<tr>
<td>SK</td>
<td>1.4</td>
<td>2.0</td>
<td>13*</td>
<td>2.4</td>
<td>11*</td>
<td>9*</td>
<td>5*</td>
<td>0.7</td>
<td>17*</td>
<td>0.1</td>
<td>3**</td>
<td></td>
<td></td>
</tr>
<tr>
<td>TA</td>
<td>0.7</td>
<td>0.4</td>
<td>9*</td>
<td>1.9</td>
<td>2.5</td>
<td>4*</td>
<td>5*</td>
<td>1.4</td>
<td>3**</td>
<td>8*</td>
<td>0.3</td>
<td>4*</td>
<td></td>
</tr>
<tr>
<td>TH</td>
<td>6*</td>
<td>0.3</td>
<td>5*</td>
<td>2.1</td>
<td>6*</td>
<td>9*</td>
<td>1.2</td>
<td>4*</td>
<td>0.5</td>
<td>1.1</td>
<td>0.9</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* Significant at the one-percent level.
** Significant at the five-percent level.

4.1. General Observations

The stock markets with significant lead/lag linkages are not good portfolio diversification prospects. The findings show that Asian stock markets have significant lead/lag linkages. The F-value statistics in Table 3 indicate that most Asian stock markets have significant influence on the other Asian stock markets (i.e., the past returns of most Asian stock markets can predict the future returns of other Asian stock markets. 65 of the 156 F-value statistics are statistically significant at the one-percent level. 18 test statistics are significant at the five-percent level.

The sum of the F-value statistics in each column of Table 3 shows the influence of each Asian stock market on the other Asian stock markets as an independent variable. The sum is the highest for the Singapore (146.5), Indian (113), and Japanese (98.6) stock markets. These stock markets appear to be the most influential stock markets in Asia. The sum is the lowest for the South Korean (17.3) and Philppine (17.4) stock markets. These stock markets appear to be the least influential stock markets in Asia.

All of the F-value statistics for the Indian stock market as an independent variable are statistically significant (i.e., the past returns of the Indian stock market leads -can predict- the stock returns of all the other Asian stock markets). Except the Thai stock market, the past returns of the Singapore stock market leads (can predict) the future stock returns of all the
other Asian stock markets. Except the Thai and Taiwanese stock markets, the past returns of the Japanese stock market lead (can predict) the future stock returns of all the other Asian stock markets. The past returns of the South Korean stock market leads (can predict) the future stock returns of only the Indian stock market. The past returns of the Philippine stock market leads (can predict) the future stock returns of only the South Korean stock market.

The horizontal sum of the F-value statistics in Table 3 shows to what extent each Asian stock market is influenced by the other Asian stock markets as a dependent variable (i.e., to what extent the future returns of an Asian market can be predicted by the past returns of the other Asian stock markets). The sum is the highest for the Shanghai (73.9), Australian (68.6), and South Korean (67.8) stock markets (i.e., these stock markets are the most influenced Asian stock markets by the other Asian stock markets). The sum is the lowest for the Japanese (32.1), Singapore (35.1), and New Zealand (36.6) stock markets (i.e., these stock markets are the least influenced Asian stock markets by the other Asian stock markets).

4.2. Australia

The returns of the Australian stock market lead the returns of the Indian, New Zealand, Philippine, and Thai stock markets (i.e., the past returns of the Australian stock market can predict the future returns of the Indian, New Zealand, Philippine, and Thai stock markets). The F statistics for these stock markets are all significant at the one-percent level.

The returns of the Australian stock market appear to follow the returns of the Indian, Japanese, Malaysian, New Zealand, Singapore, Taiwanese, and Thai stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, Singapore, Taiwanese, and Thai stock markets can predict the future returns of the Australian stock market). The F statistics for the Indian, Japanese, Malaysian, New Zealand, and Singapore stock markets are significant at the one-percent level. The F statistics for the Taiwanese and Thai stock markets are significant at the five-percent level.

4.3. Hong Kong

The returns of the Hong Kong stock market appear to lead only the returns of the Shanghai stock market (i.e., the past returns of the Hong Kong stock market can predict the future returns of only the Shanghai stock market). The F statistic is significant at the one-percent level.

The returns of the Hong Kong stock market appear to follow the returns of the Indian, Japanese, Malaysian, New Zealand, Shanghai, Singapore, and Taiwanese stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, Shanghai, Singapore, and Taiwanese stock markets can predict the future returns of the Hong Kong stock market). All F statistics are significant at the one-percent level.

4.4. India

The returns of the Indian stock market lead the returns of all the other Asian stock markets (i.e., the past returns of the Indian stock market can predict the future returns of all the other Asian stock markets). The test statistic for the New Zealand stock market is significant only at the five-percent level. The test statistics for all the other stock markets are significant at the one-percent level.
The returns of the Indian stock market appear to follow the returns of the Australian, Japanese, New Zealand, Shanghai, Singapore, and South Korean stock markets (i.e., the past returns of the Australian, Japanese, New Zealand, Shanghai, Singapore, and South Korean stock markets can predict the future returns of the Indian stock market). The test statistics for the Australian, Japanese, Shanghai, and South Korean stock markets are significant at the one-percent level. The F statistic for the Singapore stock market is significant only at the five-percent level.

### 4.5. Indonesia

The returns of the Indonesian stock market appear to lead only the returns of the Philippine and Thai stock markets (i.e., the past returns of the Indonesian stock market can predict the future returns of the Philippine and Thai stock market). The test statistic for the Thai stock market is significant at the one-percent level. The test statistic for the Philippine stock market is significant at the five-percent level.

The returns of the Indonesian stock market appear to follow the returns of the Indian, Japanese, Malaysian, New Zealand, Shanghai, Singapore, and Thai stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, Shanghai, Singapore, and Thai stock markets can predict the future returns of the Indonesian stock market). The F statistics for the Indian, Japanese, Malaysian, New Zealand, Shanghai, and Singapore stock markets are significant at the one-percent level. The F statistic for the Thai stock market is significant only at the five-percent level.

### 4.6. Japan

The returns of the Japanese stock market lead the returns of all the other Asian stock markets except the Taiwanese and Thai stock markets (i.e., the past returns of the Japanese stock market can predict the future returns of all the other Asian stock markets except the Taiwanese and Thai stock markets). The test statistics for the Australian, Hong Kong, India, Indonesian, Malaysian, New Zealand, Philippine, Shanghai, Singapore, and South Korean stock markets are all significant at the one-percent level.

The returns of the Japanese stock market appear to follow the returns of the Indian, Malaysian, New Zealand, Singapore, and Thai stock markets (i.e., the past returns of the Japanese stock market can predict the future returns of the Japanese stock market). The test statistics for the Indian and Singapore stock markets are significant at the one-percent level. The test statistics for the Malaysian, New Zealand, and Thai stock markets are significant at the five-percent level.

### 4.7. Malaysia

The returns of the Malaysian stock market lead the returns of all the other Asian stock markets except the Indian and Philippine stock markets (i.e., the past returns of the Malaysian stock market can predict the future returns of all the other Asian stock markets except the Indian and Philippine stock markets). The test statistics for the Australian, Hong Kong, Indonesian, Shanghai, Singapore, South Korean, Taiwanese, and Thai stock markets are significant at the one-percent level. The test statistics for the Japanese and New Zealand stock markets are significant at the five-percent level.
The returns of the Malaysian stock market appear to follow the returns of the Indian, Japanese, New Zealand, Shanghai, Singapore, and Taiwanese stock markets (i.e., the past returns of the Indian, Japanese, New Zealand, Shanghai, Singapore, and Taiwanese stock markets can predict the future returns of the Malaysian stock market). The test statistics for the Indian, Japanese, Shanghai, and Singapore stock markets are significant at the one-percent level. The test statistics for the New Zealand and Taiwanese stock markets are significant at the five-percent level.

4.8. New Zealand

The returns of the New Zealand stock market appear to lead the returns of all the other Asian stock markets (i.e., the past returns of the New Zealand stock market can predict the future returns of all the other Asian stock markets). The test statistics for the Australian, Hong Kong, Indian, Philippine, Shanghai, Singapore, South Korean, Taiwanese, and Thai stock markets are significant at the one-percent level. The test statistics for the Japanese and Malaysian stock markets are significant at the five-percent level.

The returns of the New Zealand stock market follow the returns of the Australian, Indian, Japanese, Malaysian, Singapore, and Thai stock markets (i.e., the past returns of the Australian, Indian, Japanese, Malaysian, Singapore, and Thai stock markets can predict the future returns of the New Zealand stock market). The test statistics for the Australian, Japanese, Singapore, and Thai stock markets are significant at the one-percent level. The test statistics for the Indian and Malaysian stock markets are significant at the five-percent level.

4.9. The Philippines

The returns of the Philippine stock market appear to lead the returns of only the South Korean stock market (i.e., the past returns of the Philippine stock market can predict the future returns of only the South Korean stock market). The test statistic for the South Korean stock market is significant at the five-percent level.

The returns of the Philippine stock market follow the returns of the Australian, Indian, Indonesian, Japanese, New Zealand, Singapore, Taiwanese, and Thai stock markets (i.e., the past returns of the Australian, Indian, Indonesian, Japanese, New Zealand, Singapore, Taiwanese, and Thai stock markets can predict the future returns of the Philippine stock market). The test statistics for the Australian, Indian, Japanese, New Zealand, and Singapore stock markets are significant at the one-percent level. The test statistics for the Indonesian and Thai stock markets are significant at the five-percent level.

4.10. Shanghai

The returns of the Shanghai stock market lead the returns of the Hong Kong, Indian, Indonesian, Malaysian, Singapore, Taiwanese, and Thai stock markets (i.e., the past returns of the Shanghai stock market can predict the future returns of the Hong Kong, Indian, Indonesian, Malaysian, Singapore, Taiwanese, and Thai stock markets). The test statistics for the Hong Kong, Indian, Indonesian, Malaysian, Singapore, and Thai stock markets are significant at the one-percent level. The test statistic for the Taiwanese stock market is significant only at the five-percent level.
The returns of the Shanghai stock market appear to follow the returns of the Indian, Japanese, Malaysian, New Zealand, Singapore, Taiwanese, and Thai stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, Singapore, Taiwanese, and Thai stock markets can predict the future returns of the Shanghai stock market). The F statistics for the Indian, Japanese, Malaysian, New Zealand, and Singapore stock markets are significant at the one-percent level. The F statistics for the Taiwanese and Thai stock markets are significant only at the five-percent level.

4.11. Singapore

The returns of the Singapore stock market lead the returns of all the other Asian stock markets except the Thai stock market (i.e., the past returns of the Malaysian stock market can predict the future returns of all the other Asian stock markets except the Thai stock market). The test statistics for the Australian, Hong Kong, Indonesian, Japanese, Malaysian, New Zealand, Philippine, Shanghai, South Korean, and Taiwanese stock markets are significant at the one-percent level. The test statistic for the Indian stock market is significant only at the five-percent level.

The returns of the Singapore stock market appear to follow the returns of the Indian, Japanese, Malaysian, New Zealand, and Shanghai stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, and Shanghai stock markets can predict the future returns of the Singapore stock market). The test statistics for all of these stock markets are significant at the one-percent level.

4.12. South Korea

The returns of the South Korean stock market appear to lead the returns of only the Indian stock market (i.e., the past returns of the South Korean stock market can predict the future returns of only the Indian stock market). The test statistic is significant at the one-percent level.

The returns of the South Korean stock market follow the returns of the Indian, Japanese, Malaysian, New Zealand, Philippine, Singapore, and Thai stock markets (i.e., the past returns of the Indian, Japanese, Malaysian, New Zealand, Philippine, Singapore, and Thai stock markets can predict the future returns of the South Korean stock market). The test statistics for the Indian, Japanese, Malaysian, New Zealand, and Singapore stock markets are significant at the one-percent level. The test statistics for the Philippine and Thai stock markets are significant at the five-percent level.

4.13. Taiwan

The returns of the Taiwanese stock market lead the returns of the Australian, Hong Kong, Malaysian, Philippine, and Shanghai stock markets (i.e., the past returns of the Taiwanese stock market can predict the future returns of the Australian, Hong Kong, Malaysian, Philippine, and Shanghai stock markets). The test statistic for the Hong Kong stock market is significant at the one-percent level. The test statistics for the other stock markets are significant at the five-percent level.

The returns of the Taiwanese stock market follow the returns of the Indian, Malaysian, New Zealand, Shanghai, Singapore, and Thai stock markets (i.e., the past returns of the
Indian, Malaysian, New Zealand, Shanghai, Singapore, and Thai stock markets can predict the future returns of the Taiwanese stock market. The test statistics for the Indian, Malaysian, New Zealand, Singapore, and Thai stock markets are significant at the one-percent level. The test statistic for the Shanghai stock market is significant only at the five-percent level.

4.14. Thailand

The returns of the Thai stock market lead the returns of the Australian, Indonesian, Japanese, New Zealand, Philippine, South Korean, and Taiwanese stock markets (i.e., the past returns of the Thai stock market can predict the future returns of the Australian, Indonesian, Japanese, New Zealand, Philippine, South Korean, and Taiwanese stock markets). The test statistics for the New Zealand, Philippine, and Taiwanese stock markets are significant at the one-percent level. The test statistics for the Australian, Indonesian, Japanese and South Korean, stock markets are significant at the five-percent level.

The returns of the Thai stock market follow the returns of the Australian, Indonesian, Japanese, New Zealand, Philippine, South Korean, and Taiwanese stock markets (i.e., the past returns of the Thai stock market can predict the future returns of the Thai stock market). The test statistics for the New Zealand, Philippine, and Taiwanese stock markets are significant at the one-percent level. The test statistic for the Australian, Indonesian, Japanese, and South Korean, stock markets are significant at the five-percent level.

5. Summary and Conclusions

In this paper, we study the contemporaneous co-movements of and the time-series lead/lag linkages between thirteen major Asian stock markets with daily returns data for the January 1, 2001-January 1, 2011 period. Our principal components analysis (PCA) results indicate that the co-movements of Asian stock markets have become closer and portfolio diversification benefits have decreased during this period. Our Granger causality (G-C) test results indicate significant lead/lag linkages between Asian stock markets. We find that the Singapore, Indian, and Japanese stock markets are the most influential and the South Korean and Philippine stock markets appear are the least influential stock markets in Asia. The Singapore, Japanese, and New Zealand stock markets are the least affected and the Shanghai, Australian, and South Korean stock markets are the most affected stock markets by the movements of the other Asian stock markets.

References


Appendix A

Principal Components Analysis

Principal Components Analysis (PCA) is a procedure that converts a set of correlated variables into a set of uncorrelated variables, which is called principal components, of low dimension. In mathematical language, PCA uses an *orthogonal linear transformation* to transform the data to a new coordinate system such that the greatest variance by any projection of the data comes to lie on the first coordinate (called the first principal component), the second greatest variance on the second coordinate, and so on.

PCA is a form of eigenvector-based multivariate analysis that involves calculation of the eigenvalue decomposition of a data covariance matrix or singular value decomposition of a data matrix. The approach helps to reveal the internal structure of the data in a way which best explains the variance in the data. PCA can provide user with most informative information by reducing a high-dimensional data space to a lower dimensional principal components.

The principal component analysis can be described as follows: Let \( \mathbf{X} = (x_1, x_2, \ldots, x_m)^T \) be an \( m \)-dimensional random vector. Without loss of generality, assume that \( \mathbf{X} \) has zero mean. Then, we can find a \( m \times m \) dimensional orthogonal linear transformation matrix \( \mathbf{P} \), that is, \( \mathbf{P}^T \mathbf{P} = \mathbf{I} \), such that

\[
\mathbf{Y} = \mathbf{P} \mathbf{X}
\]

is a diagonal matrix, with diagonal elements \( 1 \geq 2 \geq \ldots \geq s \geq s+1=0 \geq \ldots \geq m = 0 \). Mathematically, value of the diagonal of matrix \( \mathbf{P} \) is the \( i \)th largest eigenvalue of the matrix \( \mathbf{A} \). Let

\[
\mathbf{Y} = \mathbf{P} \mathbf{X} = (y_1, y_2, \ldots, y_m)^T
\]

then, the mean of \( \mathbf{Y} \) equals zero, random variables \( y_1, y_2, \ldots, y_m \) of \( \mathbf{Y} \) are independent of each other and with variance is decreasing order, since

\[
\text{Cov}(\mathbf{Y}) = \mathbb{E}(\mathbf{Y} \mathbf{Y}^T) = \mathbb{E}[(\mathbf{P} \mathbf{X})(\mathbf{P} \mathbf{X})^T] = \mathbf{P} \text{Cov}(\mathbf{X}) \mathbf{P}^T = \text{Diag}(1, 2, \ldots, m)
\]

More generally, denote that \( \mathbf{p}_i^T \) be the vector of the \( i \)th row of matrix \( \mathbf{P} \). Let \( k \) be an integer between \( 0 < k \leq m \), and \( \mathbf{Q} = (\mathbf{p}_1^T, \mathbf{p}_2^T, \ldots, \mathbf{p}_k^T)^T \) be the \( s \times m \) dimensional matrix that consists of the upper \( s \) rows from matrix \( \mathbf{P} \). We define random vector

\[
\mathbf{W} = \mathbf{Q} \mathbf{X} = (w_1, w_2, \ldots, w_k)^T
\]

Then, \( \mathbf{W} \) is a \( k \)-dimensional random vector consistent of with independent random
variable \( y_1, y_2, ..., y_k \) and

\[
\text{Cov}(W) = E(WW^T) = E[(QX)(QX)^T] = Q \text{Cov}(X) Q^T = \text{Diag}(\sigma_1, \sigma_2, ..., \sigma_k)
\]  

(A6)

Finding the Principal Components based on statistical sampling in a real application:

Suppose a set of \( n \) observations, \( x_1, x_2, ..., x_n \) is collected for the \( m \)-dimensional random variable \( X \), with each \( x_i = (x_{i1}, x_{i2}, ..., x_{im})^T \) representing a single grouped observation of the \( m \) random variables of \( X \). Without loss of generality, we assume that empirical mean of the \( n \) observations \( \{x_1, x_2, ..., x_n\} \) equals 0. That is, \( x_i = 0 \). Otherwise, we can always let \( \mu = x_i \) be a vector of algebraic mean of \( \{x_i\} \), and let \( (x_i - \mu), i = 1, 2, ..., n \).

If you want to reduce the data to obtain the first \( k \) principal components based on the observed data set, so that it can be described with only \( k \) variables, \( k < m \), write \( x_1, x_2, ..., x_n \) are \( n \) observations of column random vectors \( X \).

The statistical value of covariance of the \( n \) observation of random vector \( X \) can be calculated as

\[
V = (x_i)(x_i)^T = XX^T
\]  

(A7)

where \( X = (x_1, x_2, ..., x_n) \) as a \( m \times n \) matrix. Following above discussion (5) and (6), we are able to calculate the \( k \) principal components by letting

\[
W = QVQ^T
\]  

(A8)

One of the straightforward ways to determine the number of principal components \( k \) is as follows: For a selected value \( 0 < \alpha < 1 \), let

\[
k = \min\{j \mid \lambda(j) \geq \alpha\},
\]  

(A9)

where \( \lambda(j) = i \).

For example, for given \( \alpha = 0.8 \), then the number of principal components selected will capture at least 80% of the value of original variable.

The Kaiser’s Rule suggests that a principal component be selected unless it extracts at least as much as the equivalent of average value from the original variable. Specifically, let

\[
\lambda = \mu, \quad \text{where} \quad \mu = \mu, \quad \text{and}
\]  

(A10)

The Kaiser Criterion is to select \( k \) such that

\[
k = \max\{i \mid \lambda(i) \geq 1\}.
\]  

(A11)

Note that \( \{\lambda\} \) are the diagonal elements of covariance matrix \( \text{Cov}(Y) \) and let \( \{\sigma\} \) be the diagonal elements of Covariance matrix \( \text{Cov}(X) \), or, equivalently, variances of original random variable \( \{x_i\} \). Based on property from linear algebra, we have \( \lambda = \sigma \) Note also that \( \mu = m \) is the total number of the random variables, Kaiser’s Rule indicates that a principal component will be selected unless it extracts at least as much as the equivalent of average value of the original variable.
Appendix B

Granger Causality

Granger causality is a statistical concept of causality that helps to determine whether or not a time series can be used to provide better prediction of another time series. It was first proposed by and named after Clive W.J. Granger (Granger, 1969), a Nobel Prize winner in Economics.

Simply stated, a factor/cause X is called a Granger-cause of another factor/cause Y, if X can be considered, at least partially, a leading indicator of Y. That is, the past value of X contains additional information of predicting Y than past values of Y and/or other known existing leading indicators.

The original Granger causality is defined in the context of a linear regression. Let \{Y_t\} and \{X_t\} be two time series. Assume that \(y_t\) can be predicted by the following autoregressive model:

\[
y_t = a_0 + a_1 y_{t-1} + e_t \quad (B1)
\]

where \(e_t\) and \(e\) are residuals for the time series, and \(p \geq 1\) is the maximum number of lagged dependent variable that is significant in the model.

A time series \(\{X_t\}\) Granger-causes\(\{Y_t\}\) if it is a significant independent variable in the augmented autoregressive model of predicting \(y_t\):

\[
y_t = a + a_1 y_{t-1} + c x_{t-j} + e \quad (B2)
\]

where at least one of the \(c\) corresponding to the lagged values of series \(x\) is significantly different from zero.

An \(F\) test can be applied to testing the significance of Granger causality of \(x\) using the following hypothesis testing model:

\[
H_0: c_1 = c_2 = \ldots = c_s = 0
\]

\[
H_a: \text{Not all } c_i \text{ are equal to zero}
\]

Since the original concept of Granger causality developed in 1969, most research has been done in both model extension and applications. One of the direct extension is to define Granger causality in more general form by extending regression form (B1) and (B2) to the following more general multi-dimension forms:

\[
Y_t = A_0 + A_1 Y_{t-1} + B_1 W_{t-1} + E_t \quad (B3)
\]

\[
Y_t = A + A_1 Y_{t-1} + B_1 W_{t-1} + C X_{t-j} + E \quad (B4)
\]

Where \(\{Y_t\}, \{W_t\}\), and \(\{X_t\}\), for \(t = 1, 2, 3, \ldots\), are multi-dimensional time series, \(A, B\), and \(A_1, B_1, C\) are matrices, and, \(E_t\) and \(E\) are residuals for each time series. Whether \(X_t\) is G-cause to \(Y_t\) can be tested by an \(F\)-test for the null hypothesis that \(C = 0\).
In addition to the above extension of Granger causality concept, many researchers, such as Freiwald et al. (1999), have extended the G-causality model to non-linear environment. However, due to difficulty and complexity in implementation, the application of non-linear G-causality models is limited. Various methods have been developed to examine G-causality, with techniques extended beyond initial regression analysis to areas such as information theory and dynamic system theory. For example, spectral G-causality (Geweke, 1982) is proposed to use Fourier methods to examine G-causality in the spectral domain.

G-causality is widely used in finance. For example, in the studies by Ratner and Leal (1996) and Meric et al. (2000), if a national equity market’s index returns Granger-cause the equity markets index returns of another country (i.e., if the equity market index returns of a country can be used to predict the equity index returns of another country) is studied.

There are also growing application of G-causality in neuroscience, where it is used to identify causal interactions in neural data. Examples of application in this area can be found in Roebroeck et al. (2005) and Sato et al. (2006).
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