Determination of Factors Affecting the Price of Gold: A Study of MGARCH Model

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Abstract: Recently, increase of the gold prices attracts interest again together with the affects of the latest financial crisis. Main objective of this study is to determine factors affecting the gold prices. The study includes montly data between June, 1992 and March, 2010. Oil prices, USA exchange rate, USA inflation rate, USA real interest rate data are included in the model as variables. According to empircal findings, highest correlation is found between gold prices and USA exchange rate negatively. Secondly, a positive correlation is found between gold prices and oil prices.

Keywords: Gold Prices, Dow Jones Index, Oil Prices, MGARCH Model, CCC Model

JEL Classification: G12, C22, E31

1. Introduction

Gold is a precious metal which is used both as a property and as a financial asset. Importance of gold has come until today increasing its value and the area of usage. Gold was the fundemantal of the money system in the past and then became a reserve tool pegged to Dolar following the Bretton Woods. After 1973 some European Countries let their exchange rate float against dollar and convertibility of dolar against the gold ended and under these circumstances gold has lost the property of being a mean of exchange and become a personal saving tool and a part of Central Bank Reserves.

In the recent years, demand of gold has expanded with the widespread use of gold both in the industrial goods and in the jewelery sector. However, developments in the financial sector and the alternative financial instruments have decreased the importance of gold as a store of value. Afterwards, demand of gold tends to increase in the recent years, after the financial crises and individuals need for more secure investment tools. Consequently, price of gold boomed once again under this condition.

Objective of this study is estimating the gold prices with the variables that are addressed to affect the gold prices in the literature.

In the first part of the study, a detailed literatured review is made. Then, the model and the data set are explained. Consequently, data is anaylsed and evidence is investigated.

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2. Literature Review

There are many studies investigating the price of gold in the literature. Although various different variables are used in these studies, it is observed that gold prices are regressed against USA dollar and stock return in general.

Abken (1980), under the assumption of rational gold market, investigated how fast and at which direction the market responds to a new information, and whether the gold prices reflect the current information or whether time is needed to see the effects. For this purpose, gold prices are taken as endogenous variables and lagged values of gold prices and interest rates is taken as exogenous variables in a regression analysis. Monthly data between 1973-January and 1979-December show that the explicatoriness ratio of the regression equation is low. When similar relationship is sought between future prices and future spot prices, the explicatoriness ratio improves significantly.

Koutsoyiannis (1983) found that the gold prices are affected by the USA economy rather than worldwide economic conditions. It is stated that US dollar is the exchange rate providing the international liquidity, gold prices are expressed in US dollars and raw oil prices are quoted in US dollars. Therefore, a negative relationship between US dollar and gold prices are found.

Another study investigating the relationship between gold prices and exchange rates are made by Dooley et al. (1992). Monthly data between 1976–1990 is used to search USA, UK, France, Germany and Japan currencies. After building a VAR model, it is found that the parity between US dollar and the other currencies explain the changes in gold prices. Dooley et al. (1995) excluded the data of France and stated that the new findings coincide with the former study.

Harmston (1998), tested the relationship between UK, USA, France, Germany and Japan purchasing power parity and gold price fluctuations between 1870 and 1996. Results show that fluctuations are seen in the gold prices due to country crises and global crises but gold keeps its purchasing power being used as a store of value.

Christie-David et al. (2000) followed the news reports for 23 months between 1992 and 1995 in order to show the effects of macroeconomics news reports on gold prices. In this study, newsletters of various macroeconomic variables, lagged values of local government bonds, future prices of gold and silver is used. Consequently, it is found that all the precious metal instruments are affected positively by news about capacity use rate. Gold prices affected the news about producer price index, consumer price index and GDP and both gold and silver prices are affected by the news about unemployment ratio. Moreover, it is observed that news about budget deficits have no significant effect on gold prices.

Smith (2001) investigated the relationship between gold price and stock exchange price index using daily, weekly and monthly data beginning from 1991 to 2001. Four gold prices and six stock exchange indices were included in the study. A short run relationship was observed in the relevant period between gold price and stock exchange price index.

Smith (2002), in a further study, used the data between 1991 and 2001 in order to determine the short run and long run relationship of gold price and stock exchange prices. Three gold price values taken from London Stock Exchange at 10.30, 15.00 and end of day...
and 18 different stock exchange index, Japan, United Kingdom, Germany, France, Swiss, Netherlands, Italy, Spain, Sweden, Belgium, Finland, Denmark, Greece, Portugal, Norway, Austria, Turkey and Ireland, were tested. While a weak and negative relationship was found between gold prices and stock exchange prices in the short run, no significant relationship was observed in the long run.

Another study was made by Ghosh et al. (2002) using monthly data between 1976 and 1999 investigating the affects of worldwide inflation level, USA inflation level, worldwide income, value of US Dollar and random shocks on gold prices with a VAR model. It was concluded that gold prices are related with US Inflation level, interest rates and dollar exchange rate. Furthermore, a long run relationship was found between gold prices and US Consumer Price Index as a result of the cointegration analysis.

Vural (2003) tested the sensitivity of gold prices among various variables (USD/Euro parity, Dow Jones industrial production index, oil prices, interest rates, silver and copper prices) building a multivariate regression model using montly data between 1990 and 2003. As a result, gold prices were positively related with silver, oil and copper prices; negatively correlated with interest rates, USD/Euro parity and Dow Jones industrial production index.

Tully and Lucey (2007) used and APGARCH model in order to investigate affects of some macroeconomic variables on gold prices. In the 1984-2003 period, a relationship was found between daily and future prices of gold and US Dollar.

Sjaastad (2008) investigated the relationship between and forward gold prices and exchange rates. Spot and forward exchange rates between US Dollar, GB Pound, Japon Yen and Deutche Mark were included in the study and a high positive relationship was found between spot and forward prices. While the European Money Market was dominant in the Gold Price Market in 1990’s, later US Dollar played leading role. In addition, gold manufacturer countries like Australia, South Africa and Russia were found to have no significant affect on gold prices. Furthermore, while previous studies stated that gold was not a store of value against world wide inflation, conversly in this study gold was suggested a store of value.


Topçu (2010) examined the relationship between gold prices and Dow Jones industrial production index, US Dollar exchange rate, oil prices, US Inflation rate, Global Money Supply (M3) from 1995 to 2009. As a result of the multivariate regression analysis, returns of Dow Jones industrial production index and US Dollars positively affect the return of gold; and global Money supply negatively affects the return of gold. While a positive relationship was found between the return of oil prices and inflation and the return of gold, no statistically significant evidence was found. Similarly, a positive relationship was found between the price of gold and interest rates was found but, no statistically significant evidence was found.
3. Methodology

3.1. Data Set and Variables

In this study, an MGARCH model is tested in order to find variables affecting gold prices. Following the previous studies, oil prices, dollar index, Dow Jones Industrial Production Index, USA real interest rates and USA inflation rate are considered as the variables determining price of gold. The study includes monthly data beginning from January 1992 to March 2010. Data set can be seen in Table 1:

<table>
<thead>
<tr>
<th>Variable</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>RGOLD</td>
<td>Gold Prices</td>
</tr>
<tr>
<td>ROIL</td>
<td>Oil Prices</td>
</tr>
<tr>
<td>RUSD</td>
<td>Dollar Index</td>
</tr>
<tr>
<td>RDOW</td>
<td>Dow Jones Industrial Production Index</td>
</tr>
<tr>
<td>INT</td>
<td>Interest Rate</td>
</tr>
<tr>
<td>CPI</td>
<td>Inflation Rate</td>
</tr>
</tbody>
</table>

3.2. The Model

Linear regression model assumes that error terms of population regression function (Vi) have constant variance. This assumption is defined as homoscedasticity. But when time series analysis is considered, this assumption is violated. As a consequence, parameters may have big standard error terms and low significance. Widely used models used for modeling heteroscedasticity are Engle (1982)'s ARCH (Autoregressive conditional heteroskedasticity) model and Bollerslev (1986)'s GARCH (Generalized Autoregressive Conditional Heteroskedasticity) models. Different models such as Exponential GARCH (EGARCH), ARCH-M (ARCH in mean), T-ARCH (Threshold ARCH), C-ARCH (Junction ARCH), PARCH (Asymmetric ARCH) are derivated afterwards.

3.2.1. ARCH Model

Conditional variance term is considered under an uncertain environment. While unconditional variance is a constant in traditional model, conditional variance is defined as a function of lagged values of random variable.

An ARCH model is defined as:
Therefore, an ARCH model has zero mean, with a constant unconditional variance and unconstant conditional variance (Engle, 1982: 988-989).

### 3.2.2 GARCH Model

Beginning from Engle’s Model, Bollerslev defined conditional variance as an ARMA process;

\[ \varepsilon_i / \Psi_{t-1} \sim N(0, h_t), \]

as

\[ h_t = \alpha_0 + \sum_{i=1}^{q} \alpha_i \varepsilon_{i-t}^2 + \sum_{i=1}^{p} \beta_i h_{t-i}, \]

and

\[ = \alpha_0 + A(L)\varepsilon_t^2 + B(L)h_t, \]

where

\[ p \geq 0, \quad q>0 \]

\[ \alpha_0>0, \quad \alpha_i \geq 0, \quad i=1,\ldots,q, \]

\[ \beta_i \geq 0, \quad i=1,\ldots,p. \]

Different from the ARCH model, GARCH(p,q) process introduces the lagged conditional variance (Bollerslev, 1986: 308-309).
### 3.2.3 Multivariate GARCH Model

Multivariate GARCH model emphasizes the interaction of return volatilities of more than one variable in a constant period. It is also possible to investigate effectiveness of risk relationships among different variables. Kraft and Engle (1982) suggested the multivariate GARCH model and error terms are defined as:

\[
(u_j, t - 1, \ldots, u_j, t - p) \quad j = 1, \ldots, N
\]

With constraints in Diagonal VEC (Vector Error Correction), Engle and Kroner (1995) suggested BEKK (Baba, Engle, Kraft, Kroner) and CCC (Constant Conditional Correlations) models can be used for estimating multivariate GARCH model. A CCC model is used in this study. Bollerslev (1990) created an MGARCH model with constant correlations and proportion of conditional covariances and their conditional standard errors. With this constraint, a simpler and clear estimation becomes possible.

CCC model is defined as,

\[
H_t = D_t R D_t = \left(\rho_{ij} \sqrt{h_{ii} h_{jj}} \right);
\]

\[
D_t = diag \left(h_{11}^{1/2}, \ldots, h_{NN}^{1/2}\right)
\]

$H_{ij}$ can be defined as any univariate GARCH model and,

\[
R = \left(\rho_{ij}\right) \quad \text{is a symmetric and positive definite matrix of}
\]

\[
\rho_{ii} = 1, \forall i
\]

$R$ is a matrix including constant conditional correlations $\rho_{ij}$. Bollerslev’s CCC model defines a GARCH(1,1) model for each conditional variance of $D_t$.

This CCC model, $h_{ii} = w_i + \alpha \epsilon_i^{2}_{t-1} + \beta h_{ii,t-1}$, has $N(N + 5)/2$ parameters. $H_t$ will be positive defined if and only if all the conditional variances of N are positive and R is positivelt defined. Conditional correlations can be calculated with this model. (Bauwens, L. et al. 2003: 11).

### 4. Empirical Evidence

Volatilities of the variables are can be seen in Graph 1. RGOLD has a peak in 1999 and an increasing volatility after 2006. This series is more volatile in 2002, 2006 and 2008, and peaks are followed by deeps. It can be seen as an indicator of speculative fluctuations. Volatility of ROIL also increes after 1999 and afterwards mant peaks and deeps are observed. RUSD and RDOW series have also sharp peaks and deeps. While a non-stationary structure is observed in INT and CPI, an increasing trend is seen in CPI.
Descriptive statistics can be seen in Table 2. According to J-Bera statistic, none of the series except for RUSD has normal distribution. ROIL, RDOV and INT series are left skewed. In addition, RGOLD and ROIL series is peak and CPI and INT series is flat. Furthermore, an ARCH effect can be seen in RGOLD, ROIL and CPI series as a result of ARCH - LM test.

Augmented Dickey-Fuller (ADF) and Philips Perron (PP) tests show the stability of the series in Table 3. RGOLD, ROIL, RUSD and RDOV series are stationary and INT and CPI series are non-stationary. As a result, fist differences of INT and CPI series are used in the model.
Correlation coefficients can be seen in Table 4. RUSD has the highest correlation coefficient followed by DCPI. ROIL, RDOw and DINT series have relatively low correlation coefficients. While RUSD and RDOw series show a negative correlation, DCPI, ROIL and DINT have positive correlation.

After the determination of the correlation coefficients, a CCC model is built in order to determine the variables effecting gold prices. Reliability of the model should be tested after model estimation. Many univariate tests can be used for this aim and also a constrained number of multivariate tests can also be made. In literature, tests for evaluating conditional
variance model (heteroscedasticity X) can be divided into 3 categories: (1) Box-Pierce Ljung Portmanteau Test, (2) Tests based on error terms, (3) Lagrange Multiplies Tests (Bauwens, et al., 2003: 24-25).

In order to evaluate the estimated model, distributions of the standard errors are tested and error terms are found to have normal distribution. Distribution of the error terms are shown in Table 1. Another criterion to have an idea about this distribution is the Q-Q Graphs of the error terms. As can be seen in Appendix 2, graphs show the same result.

Q and Q^2 statistics are calculated in order to see autocorrelation and heteroscedasticity and also ARCH - LM test is consulted. Results can be seen in Table 5.

Table 5: Ljung Box Q, Q^2 and ARCH - LM Statistic of the Standard Errors

<table>
<thead>
<tr>
<th></th>
<th>RGOLD</th>
<th>ROIL</th>
<th>RUSD</th>
<th>RDOW</th>
<th>DINT</th>
<th>DCPI</th>
</tr>
</thead>
<tbody>
<tr>
<td>Q(36)</td>
<td>26.99</td>
<td>48.39</td>
<td>36.37</td>
<td>26.88</td>
<td>41.94</td>
<td>161.29</td>
</tr>
<tr>
<td>Q^2(24)</td>
<td>20.10</td>
<td>28.34</td>
<td>20.26</td>
<td>9.89</td>
<td>29.86</td>
<td>14.50</td>
</tr>
<tr>
<td>ARCH - LM</td>
<td>0.001</td>
<td>2.798</td>
<td>1.438</td>
<td>0.512</td>
<td>0.446</td>
<td>0.017</td>
</tr>
</tbody>
</table>

When we look at Q statistic, no autocorrelation can be seen between the error terms after the estimation of the model. Q^2 statistic shows that there is no heteroscedasticity problem for the error terms. For the ARCH - LM test, results of the test statistic (n.R^2) is smaller than the critical value at 0.05 significance level (3.841), consequently ARCH effect disappears.

Under these circumstances, conditional correlation coefficients of the model is calculated and shown in the Table 6:

Table 6: Conditional Correlation Coefficients

<table>
<thead>
<tr>
<th></th>
<th>RGOLD</th>
<th>ROIL</th>
<th>RUSD</th>
<th>RDOW</th>
<th>DINT</th>
<th>DCPI</th>
</tr>
</thead>
<tbody>
<tr>
<td>RGOLD</td>
<td>1.000000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>ROIL</td>
<td>0.153518</td>
<td>1.000000</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RUSD</td>
<td>-0.476277</td>
<td>-0.278687</td>
<td>1.000000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>RDOW</td>
<td>-0.079788</td>
<td>-0.001537</td>
<td>-0.128204</td>
<td>1.000000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DINT</td>
<td>-0.035815</td>
<td>0.209359</td>
<td>0.002860</td>
<td>-0.025268</td>
<td>1.000000</td>
<td></td>
</tr>
<tr>
<td>DCPI</td>
<td>0.151790</td>
<td>0.454666</td>
<td>-0.147494</td>
<td>-0.072282</td>
<td>0.099945</td>
<td>1.000000</td>
</tr>
</tbody>
</table>

When we look at the conditional correlation coefficients of the model, similar to the first calculation, RUSD has the highest correlation coefficient with a bigger and negative coefficient (-0.47). It can be seen as a negative relationship between the return of dollar and the return of gold. When we compare table 4 and table 6, it is seen that conditional correlation coefficients are 0.02 higher than the unconditional correlation coefficients.
When we compare Table 4 and Table 6, conditional correlation coefficient between the return of gold and the inflation rate decreased by 0.03 point according to unconditional correlation coefficient and become 0.15. This shows a positive and weak relationship between the return of gold and the inflation rate. Conditional correlation coefficient between the return of gold and Dow Jones Industrial Production Index (-0.07) shows “Very weak negative correlation”. These coefficients decrease by 0.04 when we compare with unconditional relationship. Conditional correlation coefficient between the return of gold and the interest rate decreased by 0.04 point according to unconditional correlation coefficient and turn to be negative, but in both cases the relationship is insignificant. While significance from the highest relationship to the lowest for unconditional correlation coefficients is RUSD, DCPI, ROIL, RDOW and DINT, for the conditional correlation coefficients it is RUSD, ROIL, DCPI, RDOW and DINT.

5. Conclusion

In this study, variables that are thought to affect the gold prices are analyzed with a MGARCH model including the data from 1992 and 2010. Oil prices, USA exchange rate, USA inflation rate, USA real interest rate data are included in the model as variables. First differences of USA exchange rate and real interest rates are taken and return series of the other variables are used. An MGARCH model is estimated by CCC model for the reason that it gives the best results for the estimation of the coefficients. According to empirical findings,
highest correlation is found between gold prices and USA exchange rate negatively. Secondly, a positive correlation is found between gold prices and oil prices.

According to the findings, a negative and significant relationship is found between the return of gold and the return of USA Dollar, the rest of the variables have no significant relationship with the return of gold. This result is valid both for the conditional and unconditional correlation relationship.

On the contrary to this study, significant relationship was found between the variables in the previous studies. But the results are similar to Topcu (2010) that found there is no significant relationship between oil prices and return of gold and inflation rate and the return of gold.

Similarly, Tully and Lucey (2007) found gold prices are the factor of USA Dollar and other variables have effects at a lower level. Results of Tully and Lucey (2007) are parallels to our study.

As a consequence, in the relevant period, return of gold show a non-linear change, in other words, market is non-linear. When the market is efficient, linearity can be considered, but when there is an inefficient market, relationships are non-linear. As a result of this study, gold market can be evaluated as inefficient. There are many studies showing the same consequences both for the developed and developing countries. On this account, this study motivates the analysis showing the non-linear relationship of the market besides the linear relationship.

References


GFMS (2010). http://www.gfms.co.uk/precious_metals минing_cost_services.htm, (08.06.2010)


Appendix 1: The Prediction of the Standardized Distribution of Error Terms obtained from the Model

RESID01

RESID02

RESID03

RESID04

RESID05

RESID06
Appendix 2: Q-Q Graphics of Standard Errors

Quantiles of RESID01
Quantiles of RESID02
Quantiles of RESID03
Quantiles of RESID04
Quantiles of RESID05
Quantiles of RESID06